

Radio Lobe Dynamics and the Environment of Microquasars

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Abstract We argue that, when compared to AGNs in dynamical terms, microquasars are found in *low* density, *low* pressure environments. Using a simple analytic model, we discuss radio lobe dynamics and emission. Dynamical considerations for GRS 1915+105 and GRO J1655–40 show that they are located in ISM densities well below the canonical $n_{\text{ISM}} \sim 1 \text{ cm}^{-3}$ unless the jets are unusually narrow or much more powerful than currently believed.

Key words. galaxies: jets – ISM: jets and outflows – stars: individual: GRS 1915+105, GRO J1655–40

1. Introduction

From the time of discovery of relativistic jets in Galactic X-ray binary sources their morphological and physical similarity with AGN jets has been stressed in the literature (see Mirabel & Rodríguez 1999, for a review on the subject). This similarity has inspired comparison of Galactic and extragalactic jets on a qualitative level.

Such comparisons are a powerful tool to study the dependence of jets on the input conditions, knowledge of which is crucial for understanding the process of jet formation. While the central black holes in AGNs span a range of 3 orders of magnitude in central mass M , with measurements of M often hampered by the lack of accurate indicators, Galactic compact objects fall into a relatively narrow range in M , while extending the mass scale to a range of over 9 orders of magnitude.

So far, the comparison has focused mainly on the emission from the inner jet, while large scale (lobe) emission has traditionally been difficult to observe in Galactic jets and has thus not been considered much in the literature. This *letter* presents arguments for the scaling expected on large scales. Section 2, reviews the scaling relations of jet parameters. In Sect. 3 we argue that, typically, microquasar jets are located in low density environments compared to AGN jets, derive simple scaling relations for radio lobes and put limits on the ISM density surrounding GRS 1915+105 and GRO J1655–40. Section 4 summarizes.

2. Scaling of jet sources

The conditions in the inner disk around black holes are essentially determined by three parameters: black hole mass M , spin a , and accretion rate $\dot{m} = \dot{M}/\dot{M}_{\text{Edd}}$ (\dot{M}_{Edd} is the Eddington rate). Jet formation seems to be strongly dependent on \dot{m} , with jet activity associated with a given

range in \dot{m} , while the influence of a is still unclear. As we are interested in powerful jets, we assume that a and \dot{m} take on their optimal value for jet formation and consider only variations in M . Then, the kinetic jet luminosity L follows $L \propto M\psi(\dot{m}, a)$, with some unknown function ψ .

We can write the scaling of physical quantities in the inner, radiation pressure dominated disk as follows: all size and time scales relate linearly to the fundamental length scale, the gravitational radius r_g of the black hole: $r \propto \tau \propto r_g \propto M$. It is convenient to define natural units $\varpi \equiv r/r_g$ and $T \equiv ct/r_g$. It follows from simple dimensional arguments, or from standard accretion disk theory (Shakura & Sunyaev 1976), that density and pressure scale inversely with M : $n_{\text{disk}} \propto p_{\text{disk}} \propto M^{-1}$. The magnetic pressure generated or transported by the disk will be some fraction φ of the gas pressure: $p_B = \varphi p_{\text{gas}} \propto M^{-1}$, thus $B \propto M^{-1/2}$; φ is arbitrary but should not depend on M . Since jets originate in the inner disk, conditions in the inner jet should assume the same scaling: The jet cross section R_0 at injection scales with M , $R_0 \propto M$, density and pressure scale like M^{-1} , and the jet power in a Poynting flux dominated jet follows $L_{\text{kin}} \propto R^2 B^2 \propto M$.

While this simple scaling might suggest that all aspects of relativistic jets should assume a simple M -dependence, this is not so. This can be seen from the observed non-linear scaling of the radio flux of the inner jet with M that has been explained successfully using only the above scaling relations and simple assumptions about jet geometry (Falcke & Biermann 1996).

In this *letter* we consider the large scale structure of jets, where interaction with the environment is important. The scaling based only on conditions in the inner disk will not hold, since parameters independent from conditions in the disk enter: external density ρ_x and pressure p_x . Since ISM densities are typically larger than IGM den-

sities (with the canonical ISM value of $n_{\text{ISM}} \sim 1 \text{ cm}^{-3}$), one might think that, compared to AGN jets, Galactic jets are situated in high density environments. In the following section, we will argue that this is a misconception and that the self-similarity in M , which seems to be describing the inner jet rather well, is broken on large scales.

3. Large scale evolution of radio sources

3.1. Radio lobe dynamics

The large scale dynamics of an *active* source (i.e., still driven by active jets) are governed by the dimensionless ratio $\eta_p \equiv (\mathcal{L}/R^2 c^3 \rho_x)$, where R is the characteristic size scale (i.e., cross section) of the jet, and \mathcal{L} is the mean kinetic luminosity¹. Since typical dimensions of the *jet* are set by the inner disk and should follow $R \propto M$ (see Sect. 2), and since $\mathcal{L} \propto M$, the problem becomes scale invariant (i.e., the value of η_p independent of M) if $\rho_x \propto M^{-1}$.

IGM densities fall into the range $10^{-5} \text{ cm}^{-3} \lesssim n_{\text{IGM}} \lesssim 10^{-2} \text{ cm}^{-3}$, while Galactic ISM densities span the range of $\text{few} \times 10^{-3} \text{ cm}^{-3} \lesssim n_{\text{ISM}} \lesssim 10^4 \text{ cm}^{-3}$ (the small value is valid for the hot ISM phase and the halo, the upper limit for densities in molecular clouds). Thus, the similarity condition $\rho_x \propto M^{-1}$ could only be satisfied for microquasars situated in molecular clouds. Most Galactic jets are, however, located in *much* lower ISM densities. Thus, compared to radio galaxies, microquasars are situated in *low* density environments in a dynamical sense.

Similarly, one can argue that microquasars are located in *low pressure* environments: The terminal size ϖ_t of an *inactive* radio lobe, when it has reached pressure equilibrium with its environment, measured in natural units, will follow $\varpi_t \sim (M p_x)^{-1/3}$. The dynamical time in natural units will be $T \propto \varpi_t / c_{s,x} \propto (M^2 \rho_x p_x)^{-1/2}$, where $c_{s,x}$ is the external sound speed. Scale invariance in M (i.e., quantities expressed in natural units are independent of M) would require $p_x \propto M^{-1}$. Since IGM and ISM pressures are comparable, microquasars are, in effect, located in low pressure environments, relative to AGN jets, and the equilibrium size and dynamical time scales are much larger than in AGNs when expressed in natural units.

Based on this premise, the dynamics of microquasar lobes might be qualitatively different from AGN lobes. Because observations of microquasar radio lobes are only just beginning to appear (partly due to their low brightness), it is unclear how to describe the dynamics of these

sources. Numerical simulations and more radio observations are therefore necessary. Meanwhile, we can use the existing framework of AGN radio lobes for simple estimates. In turn, observations of microquasars can be used to study the lobe evolution in low density environments.

Once it has passed through the terminal shock, the spent jet fuel is deposited in the vicinity of the jet head, inflating the radio lobes. During the early (i.e., active) stage, the lobes expand supersonically into the environment. Later they come into pressure equilibrium. For a supersonic bubble expanding into a medium with a radial powerlaw density profile $\rho_x \equiv \rho_{x,0} (r/r_x)^{-\zeta}$, there exists a well known self-similar solution (Castor et al. 1975; Falle 1991) for the cocoon radius r_c :

$$r_c = A \left(\frac{\mathcal{L} t^3}{\rho_x(r)} \right)^{1/5} = A \left(\frac{\mathcal{L} t^3}{\rho_{x,0} r_x^\zeta} \right)^{1/(5-\zeta)} \quad (1)$$

with $A \equiv [(5-\zeta)^3 [36\pi (8-\zeta)^{1+\zeta} (11-\zeta)^{2-\zeta}]]^{-1/5-\zeta}$ of order unity. This scaling is still appropriate if the cocoon is not spherical and entirely sufficient for our purpose.

The solution in eq. (1) is Rayleigh-Taylor unstable for $\zeta \geq 2$. However, the environments of AGNs and microquasars are benign: microquasars are typically located in homogeneous media ($\zeta \sim 0$), while AGNs are typically located in stratified atmospheres with roughly uniform densities close in and steeper decline further out ($\zeta \sim 1.5$).

If the nuclear source turns off before the lobes reach pressure equilibrium with their surroundings, a Sedov phase similar to a regular blast wave will follow, though the lobe gas will be relativistic, thus expansion will only be supersonic with respect to the external gas. If the source sits in a stratified atmosphere the lobes will rise buoyantly and cool adiabatically, once the expansion becomes subsonic (i.e., in pressure equilibrium with the environment).

3.2. Scaling relations for emission from radio lobes

Using eq. (1) one can estimate the emission from the radio lobes. For a powerlaw distribution $f(\gamma) = C\gamma^{-s}$ with spectral index $s \sim 2$ this gives (e.g., Jarvis et al. 2001):

$$L_\nu \propto \rho_x^{\frac{3+3s}{4(5-\zeta)}} r_x^{\frac{\zeta(3+3s)}{4(5-\zeta)}} \mathcal{L}^{\frac{12+(5+s)(2-\zeta)}{4(5-\zeta)}} t^{\frac{36-(5+s)(4+\zeta)}{4(5-\zeta)}}. \quad (2)$$

Using eq. (2) we can determine the scaling of radio luminosity with the fundamental source parameters. For active sources with the same *absolute* age t , the radio flux will scale like $F_\nu \propto \mathcal{L}^{1.3} \rho_x(r)^{0.45} t^{0.4} \propto M^{1.3} \rho_x(r)^{0.45}$. Typically, however, one would expect the jet activity time scale to be proportional to the disk time scales, i.e., proportional to M . Comparing sources of the same *scaled* age t/M gives $F_\nu \propto \mathcal{L}^{1.3} \rho_x^{0.45} M^{0.4} \tau^{0.4} \propto M^{1.7} \rho_x(r)^{0.45}$.

Thus, for sources located in *uniform* environments, the scaling index $\xi \equiv d \ln F_\nu / d \ln M$ will fall into the range $1.3 \leq \xi \leq 1.7$, interestingly close to the scaling measured in AGNs (e.g., Lacy et al. 2001). This limit should be valid for Galactic sources and for extragalactic sources which are still confined to the core of the cluster potential (where

¹ The evolution time scales for AGN lobes are of order $\tau \sim 10^7 - 10^8$ yrs. Variation in L_{kin} on much shorter time scales will average out, making the large scale evolution dependent only on the *mean* kinetic power $\mathcal{L} \equiv \langle L_{\text{kin}} \rangle$. Though the relation between \mathcal{L} and M is not known (possibly depending on details like binary accretion) the giant flare duration of order days observed in microquasars is only one or two orders of magnitudes shorter than the estimated life times of extragalactic jets when scaled by mass (of order $10^6 - 10^8$ yrs) and we will assume that the duty cycles and typical time scales of jet activity scale roughly linearly with M , and thus $\mathcal{L} \propto M$.

($\zeta \sim 0$). In stratified atmospheres (i.e., for large AGN jets), the dependence of F_ν on ρ_x can lead to a much weaker M dependence: for the canonical value of $\zeta \sim 1.5$, found in typical isothermal cluster atmospheres, Jarvis et al. (2001) find $\xi \sim 1.1$ for sources of the same age t , and for sources of the same *scaled* age $\xi \sim 0.9$. Finally, a useful (since measurable) comparison is for sources of the same absolute size r_c , where $\xi = (5 + s)/6$, independent of ζ .

3.3. Microquasar radio lobes

Strictly speaking, eq. (1) is valid only for lobes expanding at sub-relativistic speeds. Since, as argued in this paper, microquasars are located in under-dense environments, their expansion stays relativistic much longer, measured in natural units $T \propto t/M$, which complicates the dynamics significantly, partly because the lobes are no longer in causal contact [which was the tacit assumption in deriving eq. (1)]. An analytic treatment of the evolution of relativistic lobes is beyond the scope of this *letter*. Instead, we simply note that the following discussion applies only to microquasar lobes old enough to have become sub-relativistic. For the moderate Lorentz factors of $\Gamma_{\text{jet}} \sim 5$ involved, relativistic corrections should, in any case, stay within an order of magnitude, sufficient for the purpose of the rough estimates presented here.

We can then use eq. (2), taking a fiducial kinetic jet luminosity of $\mathcal{L} \equiv 10^{39} \mathcal{L}_{39} \text{ ergs s}^{-1}$ (a reasonable estimate during powerful flares like those observed in GRS 1915+105 or GRO J1655–40) and a constant external density with $\zeta = 0$ to arrive at an estimate of the absolute flux from a microquasar at distance $D = 10 D_{10} \text{ kpc}$ of

$$F_\nu \sim 40 \text{ mJy } n_{\text{ISM}}^{0.45} \mathcal{L}_{39}^{1.3} t^{0.4} \frac{\varphi^{3/4}}{1 + \varphi} D_{10}^{-2} \nu_5^{-1/2}, \quad (3)$$

where ν_5 is the observing frequency in units of 5 GHz.

Since the lobe expansion will be supersonic for much longer than the expected lifetime of the nuclear jet, a Sedov phase will follow the active expansion phase, during which the lobe radius will roughly follow $R \propto t^{2/5}$ and the luminosity will follow $L_\nu \propto t^{-0.9}$. This phase will begin after the source switches off, at $t_s = 10^5 \text{ s } E_{44}/\mathcal{L}_{39} \approx 1 \text{ day}$, and it will last until the source reaches pressure equilibrium with the surrounding medium at t_p .

Since the luminosity during the Sedov phase is declining, the source flux reaches a maximum at the beginning of the Sedov phase and will then follow

$$F_\nu \sim 4 \text{ Jy } \frac{n_{\text{ISM}}^{0.45} \mathcal{L}_{39}^{0.3} E_{44}^{0.4}}{D_{10}^{-2}} \frac{\varphi^{3/4}}{1 + \varphi} \left(\frac{t}{t_s} \right)^{-0.9} \nu_5^{-1/2} \quad (4)$$

with a timescale of $t_s \approx 1 \text{ day}$. For ISM densities appropriate for the hot phase, the flux should be rather dim to begin with and fade quickly beyond detectability.

For an external pressure of $p_x \equiv 10^{-12} \text{ ergs cm}^{-3} p_{-12}$, the lobe reaches pressure equilibrium with the ISM when it has reached an equilibrium size of $r_e \sim 1 \text{ pc } E_{44}^{1/3} p_{-12}^{-1/3}$ on a timescale of order $\tau_e \sim 2 \times 10^4 \text{ yrs } E_{44}^{1/3} n_x^{1/2} p_{-12}^{-5/6}$. The

radio flux is then $F_\nu \lesssim 3 \times 10^{-6} \text{ Jy } E_{44}^{7/4} p_{-12}^{-2} D_{10}^{-2} \nu_5^{-1/2}$ (the upper limit is set by equipartition), with surface brightness $I_\nu \lesssim 10^{-5} \text{ Jy arcmin}^{-2} E_{44}^{1/3} p_{-12}^{17/12} \nu_5^{-1/2}$, corresponding to a brightness temperature of $T_B \lesssim 2 \times 10^{-4} \text{ K } p_{-12}^{17/12} E_{44}^{1/3} \nu_5^{-5/2}$.

Multiple ejection events will lead to the accumulation of a faint radio halo around the source, with the value for E_{44} now reflecting the total accumulated energy in the halo in the expressions for F_ν and I_ν . Strong radiative losses in the early Sedov phase (during which no further injection of relativistic particles by the jet occurs) would limit the detectability of this halo to very low frequencies.

The lack of strong radio emission from lobes following the powerful outbursts from microquasars like GRS 1915+105 and GRO J1655–40 indicates that the surrounding density should be lower than the canonical value of 1 cm^{-3} [see eq. (4) and Sect. 3.4]. The detection of lobe emission from the neutron star Sco X-1 (at a distance of 3.2 kpc) at the $\sim 10 \text{ mJy}$ level and on timescales of order days (Fomalont et al. 2001) is also roughly consistent with originating from the early Sedov phase. Persistent radio structures on pc scales have been found in the sources 1E 1740.7–2942 (Mirabel & Rodríguez 1999) and GRS 1758–258 (Martí et al. 1998). The lack of current jet activity, compared to the relatively strong emission from the extended structure on 0.1–1 mJy levels would argue for an epoch of powerful jet activity in the recent past. The flux and surface brightness of these sources indicate that they are either located in regions of large pressure (which would be compatible with their position close to the Galactic center) and/or that the emitting plasma has not yet reached pressure equilibrium with the ISM.

3.4. The environment of GRS 1915 and GRO J1655

We shall now demonstrate that the best studied microquasars, GRS 1915+105 and GRO J1655–40, are indeed located in low density gas. For the sake of simplicity we assume that the bright knots in the jet of GRS 1915+105 are discrete ejections. Kaiser et al. (2000) have demonstrated how the physics of the jet changes if the knots are internal shocks rather than blobs. However, as long as we consider only the *total energy* E contained in the outflow, the internal jet structure is irrelevant for this argument.

VLBI and *MERLIN* observations of the 1994 and 1997 events (Mirabel & Rodríguez 1994; Fender et al. 1999) show that the knots traveled out to a distance of at least 0.04 pc (set by the detection limit, i.e., the knots might well have traveled further). The observed velocity of the components is *constant* out to at least this distance.

The length of the jet is already an indication that the interaction with the ISM must be much less efficient in this jet than it is in extragalactic objects: When scaled by central mass, the length of $l \gtrsim 0.04 \text{ pc}$ observed in GRS 1915+105 would translate to a jet length of $l \gtrsim 4 \text{ Mpc}$ for a jet with a supermassive black hole at its center, like M87 or Cyg A. This is longer than any observed AGN jets

- even in giant radio galaxies like NGC 315 (Bridle et al. 1976), and this is only a lower limit to the jet length!

Based on equipartition arguments, the kinetic energy in the ejection is roughly $E_{\text{kin}} \sim 10^{44} E_{44}$ ergs (Fender et al. 1999; Rodríguez & Mirabel 1999). As it travels downstream, we assume that the knot expands conically with an opening angle $\theta \equiv 5^\circ \theta_5$ (i.e., a half-opening angle of 2.5°), and sweeps up (or pushes aside) the ambient matter in its way (e.g., Heinz & Begelman 1999). The ejection will have been slowed down by the interaction with the external matter once it has swept up a fraction of $1/\Gamma$ of its own mass. Thus, for an external particle density of n_x , the ejection will slow down at a distance

$$d_{\text{slow}} \sim 10^{16} \text{ cm } (E_{44}/\Gamma_5^2 n_x \theta_5^2)^{1/3}, \quad (5)$$

where $\Gamma_5 \equiv \Gamma/5$ is the Lorentz factor of the jet.

Comparing this with the observed distance of the ejections, $d_{\text{obs}} \gtrsim 1.3 \times 10^{17} \text{ cm } D_{11} \sin(66^\circ)/\sin(\vartheta_{\text{LOS}})$ (where D_{11} is the distance to GRS 1915+105 in units of 11 kpc and ϑ_{LOS} the viewing angle of the jet), we arrive at the following upper limit on the external density:

$$n_x \lesssim 10^{-3} \text{ cm}^{-3} \frac{E_{44} \sin(\vartheta_{\text{LOS}})^3}{\Gamma_5^2 \theta_5^2 D_{11}^3 \sin(66^\circ)^3}. \quad (6)$$

A similar analysis can be made for the GRO J1655–40 jet, which has also been observed out to a distance of ~ 0.04 pc (Hjellming & Rupen 1995), giving the same limit. Thus, these jets must be located in environments much less dense than the canonical $n_{\text{ISM}} \sim 1 \text{ cm}^{-3}$, unless they are very narrow ($\theta \lesssim 0.15^\circ$) or very energetic, ($E \gtrsim 10^{47}$ ergs).

The simplest interpretation of this result is either (a) that GRS 1915+105 and GRO J1655–40 are located in a region occupied by the hot ISM phase, or (b) that previous activity of the jets has created an evacuated bubble around them (i.e., the plasma halo mentioned in Sect. 3.3), filled with relativistic plasma (in GRO J1655–40, which is a HMXB, the companion could also produce such a bubble via an outflow, while in the LMXB GRS 1915+105, a stellar origin of such a bubble would have to be attributed to the stellar wind or SN explosion of the progenitor). Since the energy requirements on such a bubble would only be of order 10^{41} ergs p_{-12} , this is energetically easily possible.

The limit set in eq. (6) can only be avoided if the jet were traveling down an evacuated channel, pre-existing to the outburst. The stability of such a channel (without strong jet activity keeping it open, which would be observable) inside a medium much more dense than the above limits is questionable, given that there should be precession and significant proper motion between outbursts.

A very narrow opening angle would imply that the jet material is very cold or very well confined. However, the pressure of the synchrotron emitting electrons alone is already much larger than typical ISM pressures, and an external confinement is therefore excluded. Thus, a very narrow opening angle would imply that the jet material is cold. This, in turn, would increase the energy requirements on the jet (Fender et al. 1999). Energies much larger than

10^{44} ergs, on the other hand, would require the kinetic luminosity of the central engine to severely exceed the Eddington limit $L_{\text{Edd}} \sim 10^{39} \text{ erg s}^{-1}$.

However, even if we allow for conservative lower limits on θ_5 and generous energy estimates, eq. (6) still shows that the density of the environment around the two best studied jets, GRS 1915+105 and GRO J1655–40, is much smaller than typical molecular cloud densities, which would be needed for scale invariance with typical extragalactic objects. These estimates show that measurements of the external density and the stopping distance of the jets could be used to constrain important parameters of the jet, such as the energy and the opening angle.

4. Conclusions

We have demonstrated that microquasars are typically located in much less dense environments than extragalactic in a dynamical sense. This results in a reduction of the expected emission from extended radio lobes, consistent with the rarity of such structures in powerful Galactic jet sources. It also explains the observed length of the jets in GRS 1915+105 and GRO J1655–40, $l \gtrsim 0.04$ pc, which would correspond to a jet length of 4 Mpc when scaled by M to AGN conditions. Estimates of the environmental density of these sources based on these length measurements indicate that these sources are located in environments much less dense than the canonical 1 cm^{-3} , unless the jets are very narrow or extremely energetic.

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